## Poker Hands

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A deck of cards has 52 cards, 13 numbers ( $\mathbf{A}, \mathbf{2}, \mathbf{3}, \mathbf{4}, \mathbf{5}, \mathbf{6}, \mathbf{7}, \mathbf{8}, \mathbf{9}, \mathbf{1 0}, \mathbf{J}, \mathbf{Q}, \mathbf{K})$, 4 suits (spades,clubs,hearts,diamonds). A poker hand consists of 5 cards from the deck. A pair means two cards have the same number. Three of a kind, means three of the same number, similarly defined for four of a kind. A Full House is when the poker hand consists of a three-of-a-kind and a pair (example AA222). A straight means you have five consecutive numbers, the first possible straight is $\mathbf{A}-\mathbf{2 - 3 - 4 - 5}$, the last one is $\mathbf{1 0 - J}-\mathrm{Q}-\mathrm{K}-\mathbf{A}$. A flush means the five cards are of the same suit. A straight flush means the hand is both a flush and a straight.

1. How many poker hands are there? (For example, one poker hand is A of hearts, $\mathbf{2}$ of spades, $\mathbf{J}$ of hearts, $\mathbf{5}$ of clubs and $\mathbf{A}$ of diamonds.
2. How many poker hands are there with just one pair?
3. How many poker hands with two pairs are there?
4. How many poker hands with three of a kind are there (and not a full house)?
5. How many poker hands with four of a kind are there?
6. How many poker hands are a full house?
7. How many poker hands are a straight flush?
8. How many poker hands are a straight but not a flush?
9. How many poker hands are a flush but not a straight?
10. How many poker hands are left (no pair, no flush, no straight)?
11. Can you give a hierarchy to the poker hands from less common to most common?
